



Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

I declare this is my own work.

AS

FURTHER MATHEMATICS

Paper 2 Discrete

Friday 16 May 2025

Afternoon

Time allowed: 1 hour 30 minutes

Materials

- You must have the AQA Formulae and statistical tables booklet for A-level Mathematics and A-level Further Mathematics.
- You should have a graphical or scientific calculator that meets the requirements of the specification.
- You must ensure you have the other optional Question Paper/Answer Book for which you are entered (**either** Mechanics **or** Statistics). You will have 1 hour 30 minutes to complete **both** papers.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page or on blank pages.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 40.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
TOTAL	



J U N 2 5 7 3 6 6 2 D 0 1

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Answer **all** questions in the spaces provided.

- 1** A student is solving a network flow problem involving water pipes.
- They have correctly found a flow through the network of $36 \text{ m}^3 \text{ s}^{-1}$
- They have correctly found a cut of the network with value $36 \text{ m}^3 \text{ s}^{-1}$
- Which one of the following is correct?
- Tick (✓) **one** box.

[1 mark]

The maximum flow through the network is less than $36 \text{ m}^3 \text{ s}^{-1}$

☐

The maximum flow through the network is equal to $36 \text{ m}^3 \text{ s}^{-1}$

☐

The maximum flow through the network is greater than $36 \text{ m}^3 \text{ s}^{-1}$

☐

It is not possible to make a conclusion about the maximum flow through the network.

☐

2 A simple-connected graph has n vertices, where $n \geq 2$

State the **minimum** number of edges of the graph.

Circle your answer.

[1 mark]

$$n - 1$$

$$n$$

$$n + 1$$

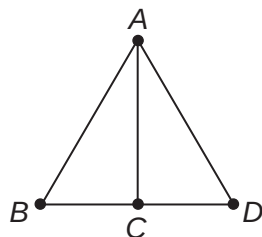
$$\frac{n(n-1)}{2}$$

Turn over for the next question

Turn over ►



3 A graph is shown below.



3 (a) Complete the table, to show the degree of each vertex.

[1 mark]

Vertex	Degree
A	
B	
C	
D	

3 (b) A student makes two statements about the graph.

Statement 1: The graph is Eulerian.

Statement 2: The graph can be drawn in one go without taking the pencil off the paper and without retracing any edges.

3 (b) (i) State, with a reason, whether **Statement 1** is correct or incorrect.

[1 mark]

3 (b) (ii) Write down a path to show that **Statement 2** is correct.

[1 mark]



- 4** A company employs five people Alisha, Gary, Jo, Sarif and Ted to complete a project. This project comprises five tasks V, W, X, Y and Z which must all be completed. Each person is to be assigned exactly one task.

The table shows the tasks to which each person could possibly be assigned.

Person	Task
Alisha	V, X, Y
Gary	W, Y
Jo	V, Z
Sarif	V, W, X
Ted	Y

- 4 (a)** Draw a bipartite graph to show this information.

[2 marks]

- 4 (b)** Find all possible ways that each person can be assigned to exactly one task to complete the project.

[2 marks]

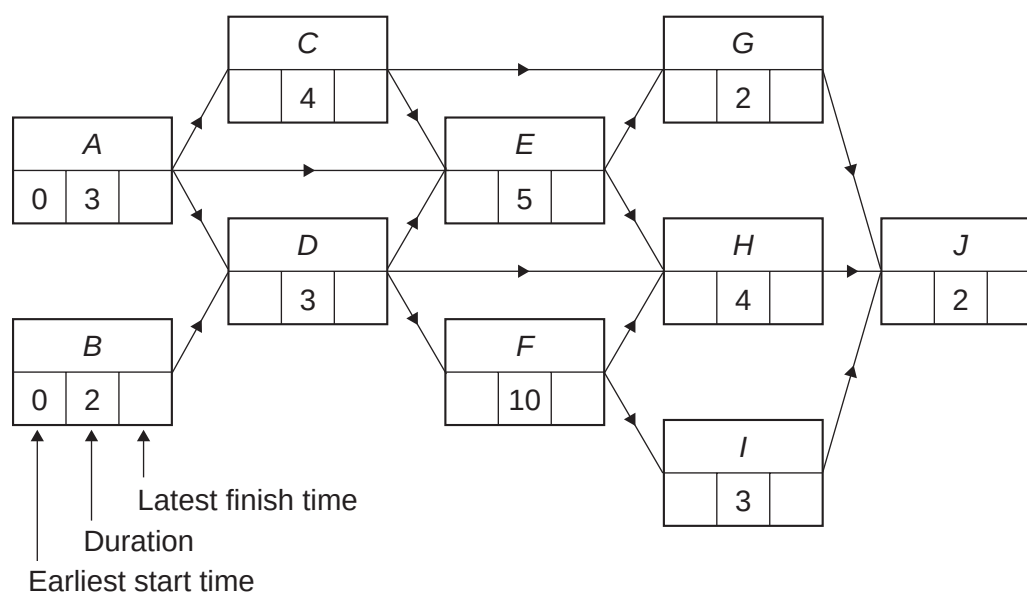
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- 5 A project consists of 10 activities A, B, C, D, E, F, G, H, I and J

The activity network for the project along with the duration, in days, of each activity is shown in **Figure 1**

Figure 1



- 5 (a) Complete the activity network in **Figure 1** by showing the earliest start time and the latest finish time for each activity.

[3 marks]

- 5 (b) Due to problems with the weather, the project manager predicts that the duration of activity E will increase by up to 7 days.

Explain whether the minimum completion time of the project increases.

[2 marks]



6 The set S is defined as $S = \left\{ x \in \mathbb{R} : x \neq \frac{1}{2} \right\}$

The binary operation $*$ is defined as

$$a * b = a + b - 2ab$$

where a and $b \in S$

It is given that S has exactly one identity element under the binary operation $*$

6 (a) Show that 0 is the identity element of S under the binary operation $*$

[2 marks]

6 (b) Find an expression for a^{-1} , the inverse of the element a , in S under the binary operation $*$

[2 marks]

Turn over ►



7 Maria is planning a tour of six towns A , B , C , D , E and F

On the tour, Maria will visit each town at least once, starting and finishing at A

Maria's aim is to minimise the total distance travelled on the tour.

The table shows the shortest distances, in miles, between each pair of towns.

	A	B	C	D	E	F
A	–	16	19	22	24	18
B	16	–	17	14	28	23
C	19	17	–	30	21	27
D	22	14	30	–	15	21
E	24	28	21	15	–	25
F	18	23	27	21	25	–

7 (a) Using the nearest neighbour algorithm starting from A , find an upper bound for the total distance travelled by Maria on the tour.

[2 marks]



- 8** A linear programming problem is represented by the following:

$$\text{Maximise } P = 3x + 2y$$

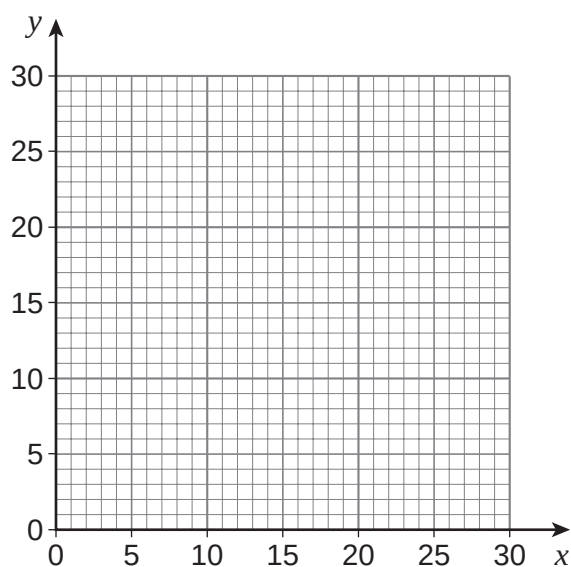
$$\text{subject to } x + y \leq 20$$

$$3x + y \geq 30$$

$$2y \geq x$$

- 8 (a)** Draw the feasible region R for the linear programming problem on the axes.

[4 marks]





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8 (b) Solve the linear programming problem, stating the values of x , y and P

[3 marks]

Turn over for the next question

Turn over ►



9 Caroline and David play a zero-sum game.

The constant k is such that $0 < k < 3$

The game is represented by the following pay-off matrix for Caroline.

		David		
Caroline	Strategy	D_1	D_2	D_3
	C_1	3	-2	-1
	C_2	-2	$k + 1$	$k + 2$
	C_3	2	4	5

9 (a) Show that the game does **not** have a stable solution.

[3 marks]



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