



GCE AS/A LEVEL

2300U20-1

WEDNESDAY, 8 JUNE 2022 – AFTERNOON

MATHEMATICS – AS unit 2

APPLIED MATHEMATICS A

**1 hour 45 minutes plus your additional
time allowance**

ADDITIONAL MATERIALS

In addition to this examination paper, you will need:

- **a WJEC pink 16-page answer booklet;**
- **a Formula Booklet;**
- **a calculator;**
- **statistical tables (RND/WJEC Publications).**

INSTRUCTIONS TO CANDIDATES

Use black ink, black ball-point pen or your usual method. You may use a pencil for graphs and diagrams only.

Answer ALL questions.

Write your answers in the separate answer booklet provided, following the instructions on the front of the answer booklet.

(Turn over)

Use both sides of the paper. Please only write within the white areas of the booklet.

Write the question number in the left-hand margin at the start of each answer.

Write the sub parts, e.g. (a), (b) and (c), within the white areas of the booklet.

Leave at least two line spaces between each answer.

Take g as 9.8 ms^{-2}

Sufficient working must be shown to demonstrate the MATHEMATICAL method employed.

Answers without working may not gain full credit.

(Turn over)

Unless the degree of accuracy is stated in the question, answers should be rounded appropriately.

INFORMATION FOR CANDIDATES

The maximum mark for this paper is 75.

The number of marks is given in brackets at the end of each question or part-question.

You are reminded of the necessity for good English and orderly presentation in your answers.

(Turn over)

REMINDER: Sufficient working must be shown to demonstrate the **MATHEMATICAL** method employed.

SECTION A: STATISTICS

01. The events **A** and **B** are such that

$$P(A) = 0.3$$

$$P(B) = 0.6$$

$$P(A \cup B) = 0.82$$

(a) Determine whether or not **A** and **B** are independent. **[4 marks]**

(b) Find the probability that exactly one of **A** and **B** occurs. **[3 marks]**

(Turn over)

02. The probability distribution for X , the lifetime of a light bulb, in hours, is given below.

X	Probability
$256 \leq x < 259$	0.05
$259 \leq x < 262$	0.25
$262 \leq x < 265$	0.45
$265 \leq x < 267$	0.20
$267 \leq x < 300$	0.05

(Turn over)

02 (a)

Suppose that a random sample of 40 light bulbs is tested, and a histogram is drawn of their lifetimes. Calculate the expected height of the bar for the interval
 $262 \leq x < 265$ **[2 marks]**

(b) Now suppose that the last two intervals are changed to
 $265 \leq x < 268$ and
 $268 \leq x < 300$

Explain why it is not possible to tell what will happen to the expected heights of the last two bars. [1 mark]

(Turn over)

- (c) Celyn collects a different random sample of 40 light bulbs to test. She draws a histogram of their lifetimes and finds that it is different to the histogram referred to in part (a). Should Celyn be concerned that the two histograms are different?**

[1 mark]

- 03.** In a study, samples of soil were collected during the summer. Soil samples of dimensions **$25\text{ cm} \times 25\text{ cm} \times 40\text{ cm}$** were collected for analysis. The study found that there were, on average, **11** earthworms per sample.
- (a)** Explain briefly the conditions under which a Poisson distribution could be used to model the number of earthworms per sample. [1 mark]
- (b)** In July, pupils at a primary school are asked to dig a smaller hole, **$25\text{ cm} \times 25\text{ cm} \times 10\text{ cm}$** and to count the number of earthworms they find. Calculate the probability that the pupils find exactly **5** earthworms. [3 marks]

(Turn over)

03. (c)

In the autumn, the average number of earthworms per sample is greater than in the summer. The probability that, in the autumn, there are fewer than 13 earthworms in a soil sample of dimensions

25 cm × 25 cm × 40 cm is

close to 36%. Find the mean number of earthworms, to the nearest whole number, per

25 cm × 25 cm × 40 cm soil sample in the autumn.

[2 marks]

04. Jessica is studying the relationship between hip girth, h cm, and thigh girth, t cm, for American adults who are physically active. She takes a random sample of 11 people from a very large dataset which she has downloaded into a spreadsheet software package. The results are shown on the next page.

<i>h</i> (cm)	<i>t</i> (cm)
98·6	48·3
112·1	87·2
97·9	55·2
110·2	68·0
89·2	48·5
111·7	63·2
87·0	49·5
94·7	55·7
100·4	59·1
104·0	64·0
88·4	52·4

04. (a)

Jessica notes that, for the thigh girth data, the lower quartile is 49.5 and the upper quartile is 64.0

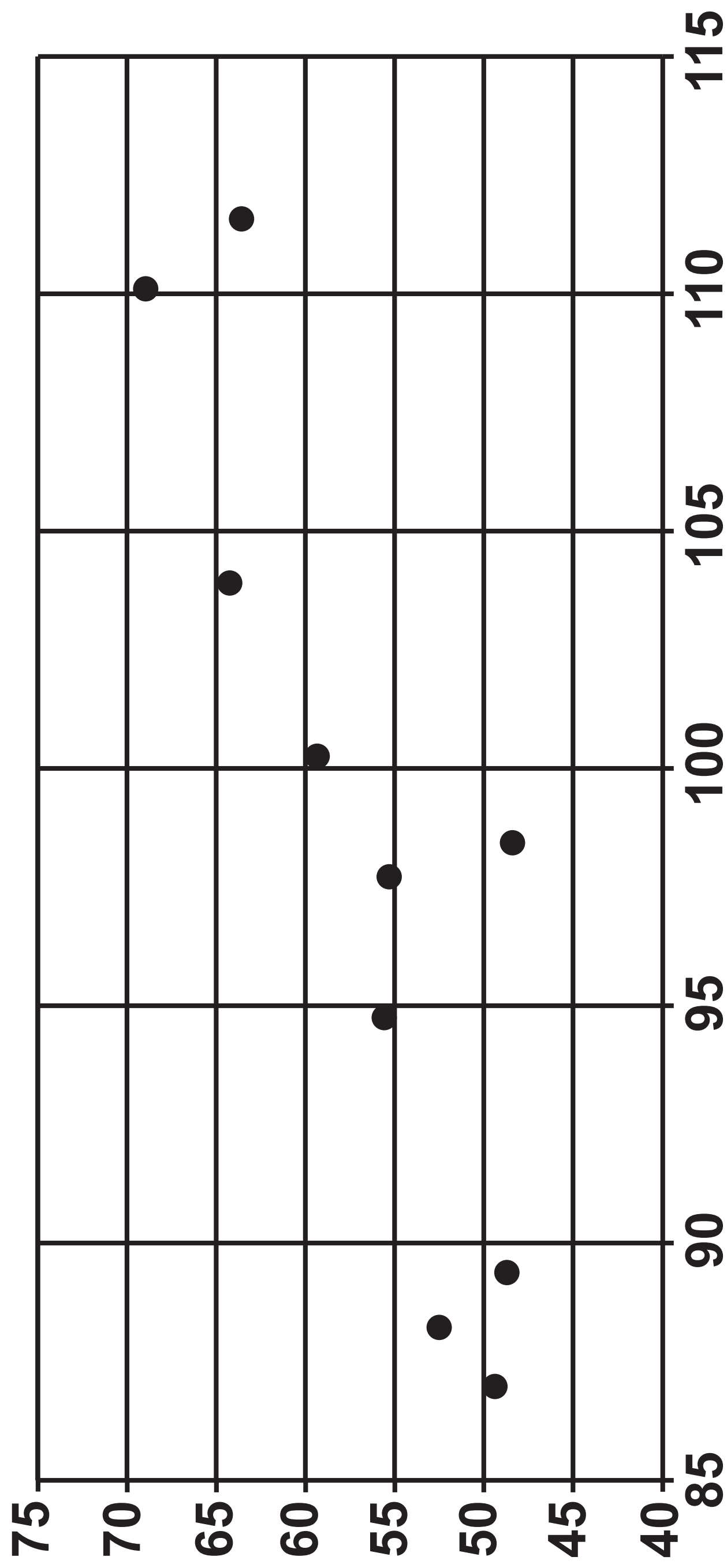
(i) Show that 87.2 should be classified as an outlier for t

(ii) Give a reason why Jessica might exclude the outlier.

(iii) Give a reason why Jessica might include the outlier. [4 marks]

THIGH GIRTH VERSUS HIP GIRTH

Thigh girth (cm)



Hip girth (cm)

- 04. Jessica decides to exclude the outlier and produces the scatter diagram opposite.**
- (b) Interpret, in context, the correlation in the data shown in the diagram.**
- [1 mark]**

The equation of the regression line of t on h for this sample is

$$**$t = 0.69h - 11.26$**$$

- (c) Interpret the gradient of the regression line in this context.**
- [1 mark]**

(Turn over)

04. (d)

Use your knowledge of large data sets and spreadsheet software packages to suggest a way in which Jessica could improve her investigation.

[1 mark]

- 05. A company, Run4Lyfe, sponsors an athletic event. The organisers of the event claim that 70% of the participants know the name of the sponsoring company. Run4Lyfe is concerned that the proportion, p , of participants knowing the name of the sponsoring company is less than 70%. They decide to survey 60 randomly selected participants to carry out a significance test.**
- (a) State suitable hypotheses for carrying out the test. [1 mark]**

05. (b) (i)

Explain what is meant by the critical region for this test.

(ii) Determine the critical region if the test is to be carried out at a significance level as close as possible to, but not exceeding, 5%.

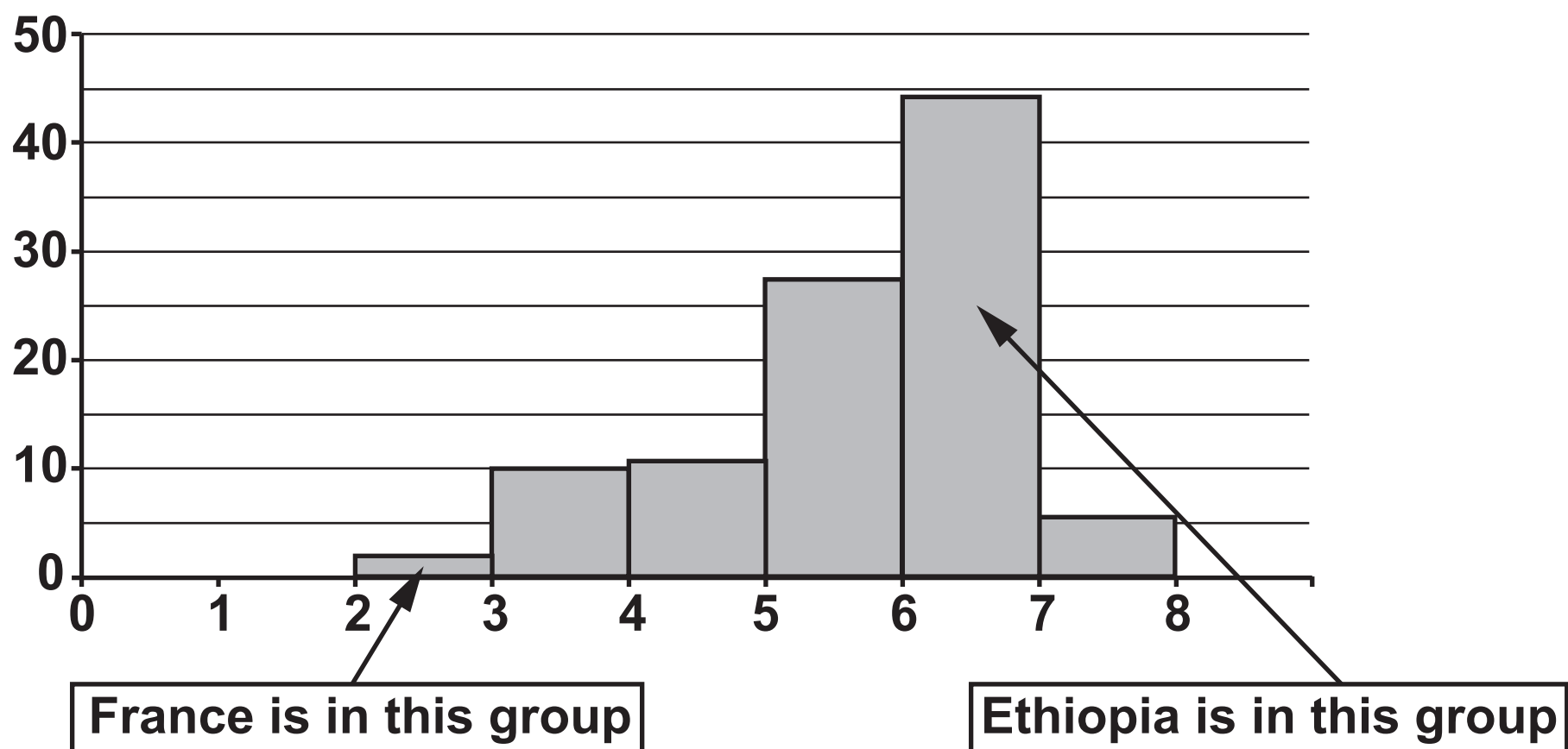
(iii) Given that 40 participants out of the 60 in the sample know the name of the company, complete the significance test. [6 marks]

(c) State, with a reason, how you would advise Run4Lyfe with regards to sponsoring the event next year. [1 mark]

(Turn over)

FERTILITY RATES IN 1914

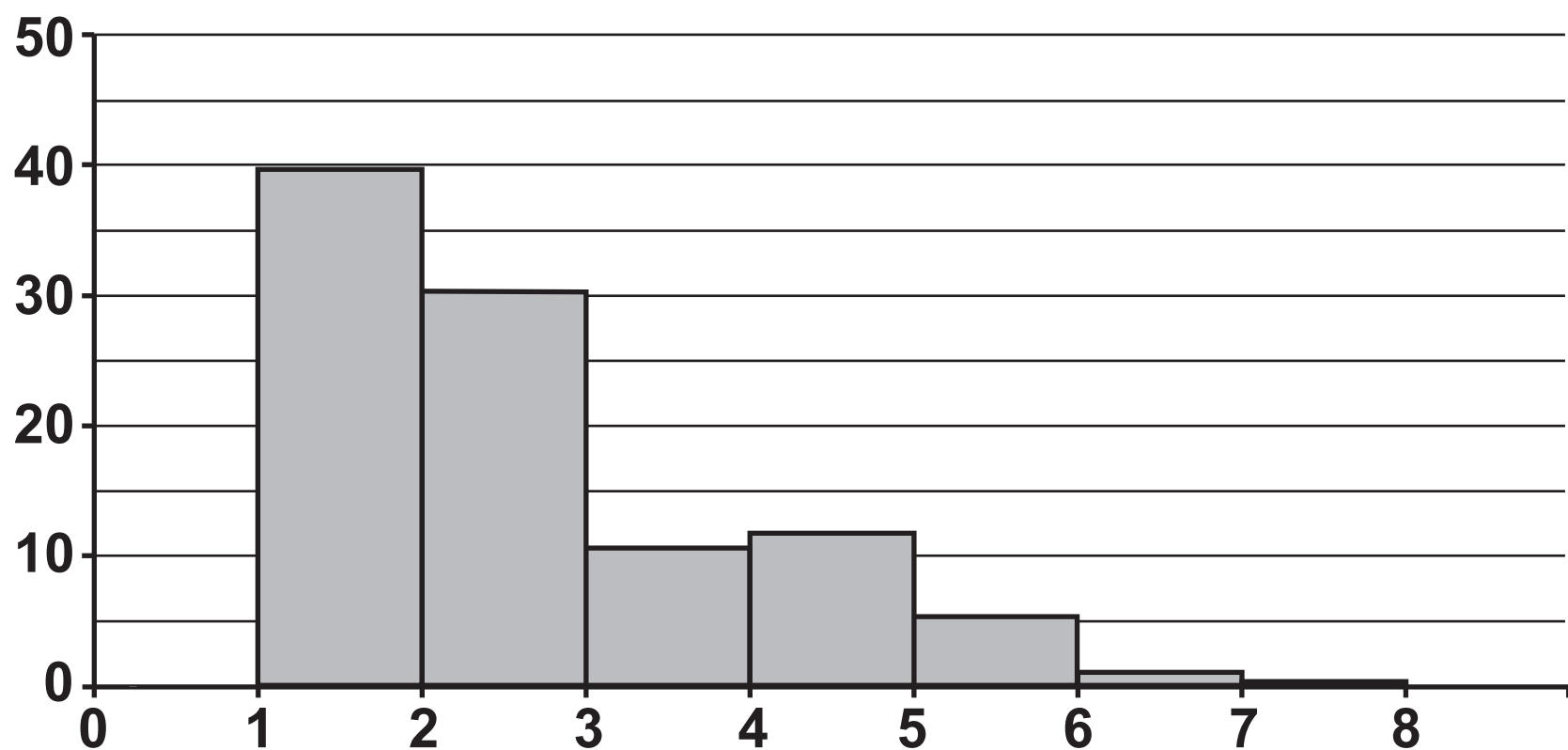
Percentage



Fertility rate

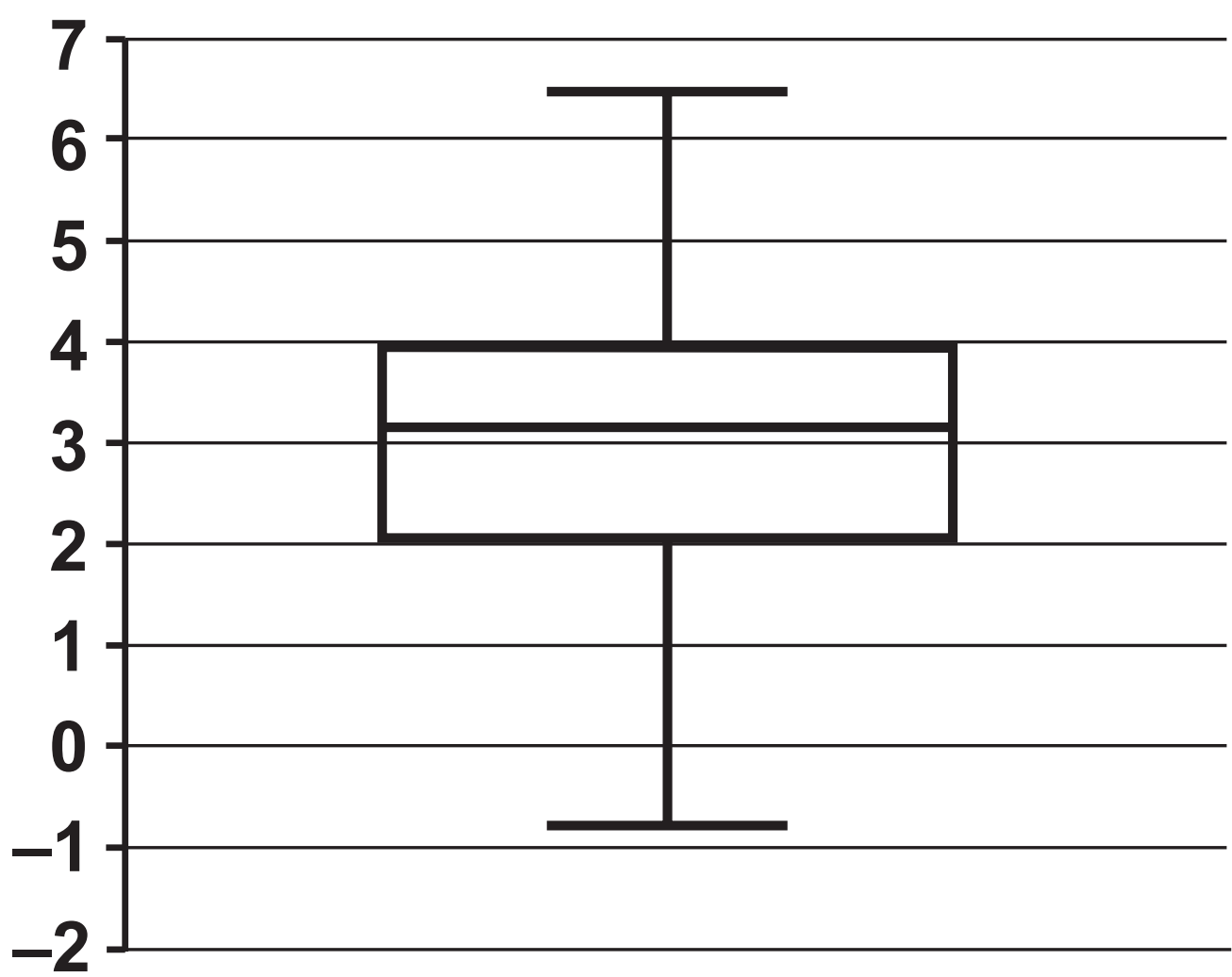
FERTILITY RATES IN 2014

Percentage



Fertility rate

DECREASES IN FERTILITY
RATES FROM 1914 TO 2014



DECREASES IN FERTILITY RATES FROM 1914 TO 2014, <i>n</i> = 197	
Minimum value	-0.71
Lower quartile	2.08
Median	3.19
Upper quartile	3.94
Maximum value	6.49

- 06. The fertility rate for a country is the average number of children that are born to a woman over her lifetime. The graphs and table opposite show some data on the fertility rates for 197 countries in the years 1914 and 2014.**
- (a) Comment on the shapes of the distributions of fertility rates for 1914 and 2014. [2 marks]**
- (b) Interpret the minimum value, -0.71 in the boxplot. [1 mark]**

06. You are also given the following information:

COUNTRY	FERTILITY RATE FOR 1914	FERTILITY RATE FOR 2014
France	Between 2 and 3	1.98
Ethiopia	Between 6 and 7	4.4

(c) (i)

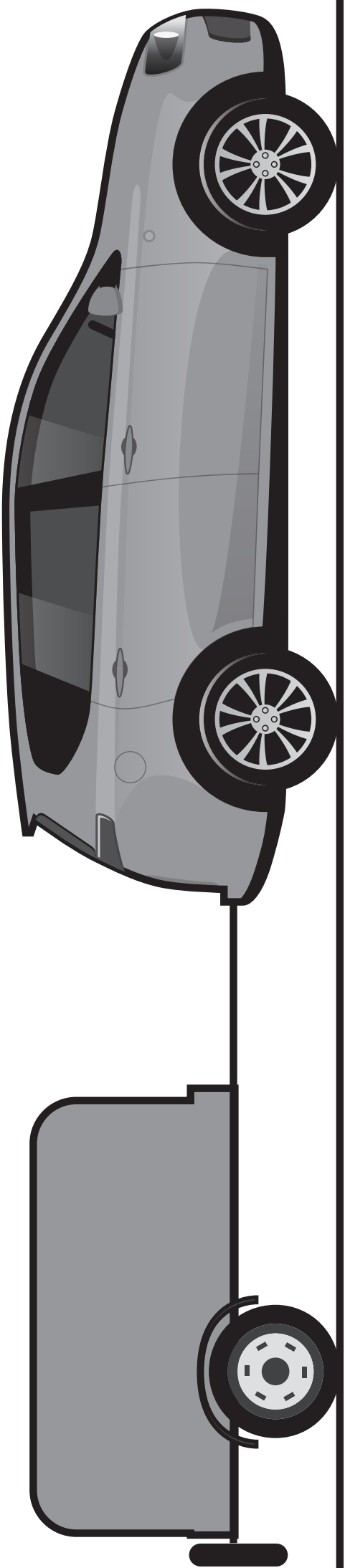
Find the best possible estimate for the decrease in the fertility rate from 1914 to 2014 for France.

(Turn over)

06. (c) (ii)

Find the best possible estimate for the decrease in the fertility rate from 1914 to 2014 for Ethiopia.

- (iii) Give one possible reason why the answers to (i) and (ii) are so different.**
- (iv) Explain why these estimates may not be very accurate. [5 marks]**



SECTION B: MECHANICS

- 07.** The diagram opposite shows a vehicle of mass **1300 kg** towing a trailer of mass **500 kg** by means of a light horizontal tow bar. The vehicle is moving forward along a straight horizontal road such that a constant resistance of magnitude **650 N** acts on the vehicle and a constant resistance of magnitude **320 N** acts on the trailer. The vehicle's engine produces a constant driving force of **F N**

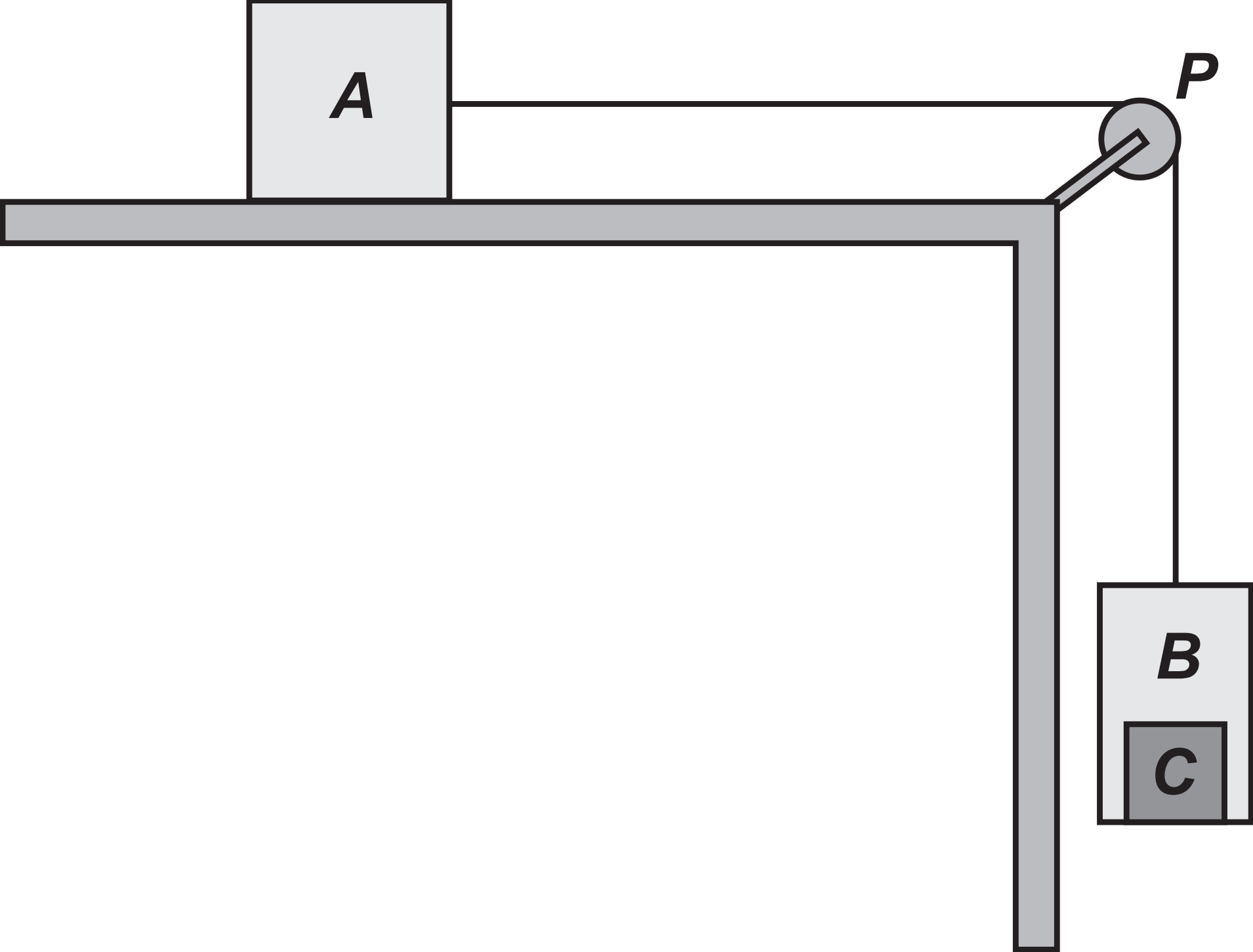
Given that the acceleration of the vehicle and trailer is **0.85 ms^{-2}** show that **$F = 2500$** and determine the tension in the tow bar.

[6 marks]

(Turn over)

- 08.** An aircraft moves along a straight horizontal runway with a constant acceleration of 1.5 ms^{-2} . Points **A** and **B** lie on the runway. The aircraft passes **A** with speed 4 ms^{-1} and its speed at **B** must be at least 78 ms^{-1} if it is to take off successfully.
- (a)** Find the speed of the aircraft 8 seconds after it passes **A** [2 marks]
- (b)** Determine the minimum value of the distance **AB** for the aircraft to take off successfully. [3 marks]

(Turn over)



09. The diagram opposite shows an object ***A***, of mass **15 kg**, lying on a smooth horizontal surface. It is connected to a box ***B*** by a light inextensible string which passes over a smooth pulley ***P***, fixed at the edge of the surface, so that box ***B*** hangs freely. An object ***C*** lies on the horizontal floor of box ***B*** so that the combined mass of ***B*** and ***C*** is **10 kg**

Initially, the system is held at rest with the string just taut. A horizontal force of magnitude **150 N** is then applied to ***A*** in the direction ***PA*** so that box ***B*** is raised.

(Turn over)

09. (a)

Find the magnitude of the acceleration of A and the tension in the string. [6 marks]

(b) Given that object C has mass 4 kg calculate the reaction of the floor of the box on object C [3 marks]

(Turn over)

10. In this question, $\underline{i}$ and $\underline{j}$ represent unit vectors due east and due north respectively.

Sarah is going for a walk. She leaves her house and walks directly to the shop. She then walks directly from the shop to the park. Relative to her house:

- the shop has position vector

$$\left(-\frac{2}{3}\underline{j}\right) \text{ km}$$

- the park is 2 km away on a bearing of 060°

(Turn over)

10. (a)

Show that the position vector of the park relative to the house

is $(\sqrt{3} \underline{i} + \underline{j})$ km

[2 marks]

(b) Determine the total distance walked by Sarah from her house to the park.

[3 marks]

(c) By considering a modelling assumption you have made, explain why the answer you found in part (b) may not be the actual distance that Sarah walked.

[1 mark]

(Turn over)

11. A particle P moves along the X -axis so that its velocity $v \text{ ms}^{-1}$ at time t seconds ($t \geq 0$) is given by

$$v = 3t^2 - 24t + 36$$

- (a) Find the values of t when P is instantaneously at rest. [2 marks]
- (b) Calculate the total distance travelled by the particle P whilst its velocity is decreasing. [7 marks]

END OF PAPER